Effect of the Accelerometer Calibration Method on AIUB’s GRACE Monthly Gravity Field Solution

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Introduction

**GRACE Mission by NASA/DLR**

- GPS Measurements + K-band Measurements + other Measurements

- Monthly Gravity Field Solutions
One of the Methods to Improve the Quality is

**Accelerometer Data Calibration**

- **On-board Accelerometer**
  - Measuring nongravitational forces acting on the satellites
    (e.g. perturbing forces by air drag, ...)

- **Official GRACE ACC1B Data**
  - contain instrument scale and bias in the linear accelerations
  → Calibration is required.

Image Courtesy GFZ
Objective

GRACE monthly gravity field solutions by the *AIUB Processing Center*

- estimates the scaling factors in three directions since the release 2 monthly gravity field solutions (*Meyer* et al. 2016) using Celestial Mechanics Approach (*Beutler* et al. 2010a, 2010b)

- To investigate the effect of the accelerometer data calibration in the Celestial Mechanics Approach using the stochastic pulses/piece-wise constant accelerations
  - Interactions between the stochastic parameters and the scaling factors for the accelerometer data calibration
Method: Accelerometer Data Calibration

• Calibration equation: \( \mathbf{a}_{\text{Calibrated}} = \mathbf{S} \cdot \mathbf{a}_{\text{Measured}} + \mathbf{b} \)

  \( \mathbf{a}_{\text{Calibrated}} \): Calibrated Acceleration  
  \( \mathbf{a}_{\text{Measured}} \): Measured Acceleration by the GRACE accelerometers  
  \( \mathbf{S} \): Scale matrix  
  \( \mathbf{b} \): bias

• Scaling Matrix:

\[
\mathbf{S} = \begin{bmatrix}
S_x & S_{xy} & S_{xz} \\
S_{yx} & S_y & S_{yz} \\
S_{zx} & S_{zy} & S_z
\end{bmatrix}
\]

  – Main diagonals: estimated once per day  
  – Usually, the off-diagonal terms are assumed to be 0:

\[
S_{xy} = S_{xz} = S_{yx} = S_{yz} = S_{zx} = S_{zy} = 0
\]
Celestial Mechanics Approach (CMA)

- A processing method to produce gravity field solutions as well as satellite orbits (Beutler et al. 2010a, 2010b)
- Used at the AIUB processing center via the Bernese GNSS Software
- Stochastic parameters

Stochastic Pulse/Piece-wise Constant Accelerations

- CMA-specific parameters:
  - Instantaneous velocity changes in three directions at particular epochs or
  - Piece-wise constant accelerations in three directions over a certain time interval

- Stochastic pulse/Piece-wise constant acceleration is varied by constraint of RMS and frequency (every 15 minutes for the GRACE orbits)
## Processing Details

<table>
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<tr>
<th>Type/Models</th>
<th>Details</th>
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</table>
| **Reference Frame**          | - Satellite RSW frame  
- GRACE Instrument (Accelerometer) frame  
- ECI J2000                                                                  |
| **Processing Strategy (SW)** | Celestial Mechanics Approach (Bernese GNSS Software)                           |
| **Estimated Parameters**     | - GRACE Orbital Elements  
- 3-dimensional Scaling Factors (Once per day) and Offsets (Once per day) for Accelerometer Data Calibration  
- Stochastic Pulses (every 15 minutes)                                     |
| **Input Data and Models**    | (Identical to AIUB GRACE Monthly Gravity Fields Release 2: Meyer et al. 2016)  
TIDE2000  
EOT11A (100)  
Desai (100)  
AOD1B (RL05)  
DE405  
IERS2010  
IERS2010  
AIUB’s a priori Model (AIUB-GRACE03S)  
GRACE ACC1B Data                                                              |
| **Time Span**                | January 2007 (1 Month)                                                  |
Stochastic Pulses ⇔ Estimated Scaling Factors (1 Month)

<table>
<thead>
<tr>
<th>Pulse Constraints (m/sec)</th>
<th>Estimated Scale Factor (Daily in January 2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 x 10^{-8}</td>
<td><img src="image1" alt="Graph for 1 x 10^{-8}" /></td>
</tr>
<tr>
<td>3 x 10^{-9}</td>
<td><img src="image2" alt="Graph for 3 x 10^{-9}" /></td>
</tr>
<tr>
<td>8 x 10^{-10}</td>
<td><img src="image3" alt="Graph for 8 x 10^{-10}" /></td>
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</tbody>
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- Smaller constraints to control overall RMS of the stochastic pulses result in the estimated scale factors which are closer to the nominal value, 1.
Stochastic Parameters (01 January 2007)

- Four different RMS constraints for the stochastic parameters:
  \[1 \times 10^{-8}, 3 \times 10^{-9}, 8 \times 10^{-10}, 3 \times 10^{-12} \text{ [m/s}^2\text{]}\]
- Magnitude of the stochastic parameters (piece-wise constant accelerations) are constrained by the pre-defined constraints.
Residuals (1): by Pulse Constraints (01 January 2007)

- **When the pulse constraints decreases, the residuals increases.**

  → The pulse constraints cannot be very small, but should be adjusted: $1 \times 10^{-9} \sim 3 \times 10^{-9}$ m/s$^2$ is reasonable level of the piece-wise constant accelerations.
Residuals (2): by each Direction (01 January 2007)

- Radial direction shows larger residuals than the other directions → related to the estimated scale factor in the radial direction closer to 1 than those in other directions
Conclusions

• In the Celestical Mechanice Approach to produce GRACE gravity field solutions, the magnitudes of contraints to the RMS of the stochastic pulses affect the estimated scaling factors for the accelerometer data calibration directly.

• Considering the reasonable levels of the residuals and the stochastic pulses to absorb the model deficiencies in the orbit determination, a value in the range $1 \times 10^{-9} \sim 3 \times 10^{-9}$ m/s$^2$ has to be selected for the constraints of the RMS of the stochastic parameters.

• Further improvements in the method of the estimation of the scaling factors used for the accelerometer data calibration are expected to improve at least certain coefficients of the monthly gravity field solutions in the gravity field using the Celestial Mechanics Approach.
Reference


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EGSIEM Project

- **European Gravity Service for Improved Emergency Management**
- Consortium
- Main Objectives:
  - Combination Service of GRACE Gravity Field Solutions
  - Near-real time Service of GRACE Gravity Field Solutions
  - Early Warning Service of Hydrological Events
- For more information: visit the website www.egsiem.eu