

# Combined SLR-derived gravity fields for EGSIEM

Mathis Bloßfeld, Andrea Grahl, Daniel König, Krzysztof Sosnica, Sandro Krauss,  
Rolf König, Jean-Michel Lemoine, Toshimichi Otsubo

Deutsches Geodätisches Forschungsinstitut (DGFI-TUM)  
Technische Universität München

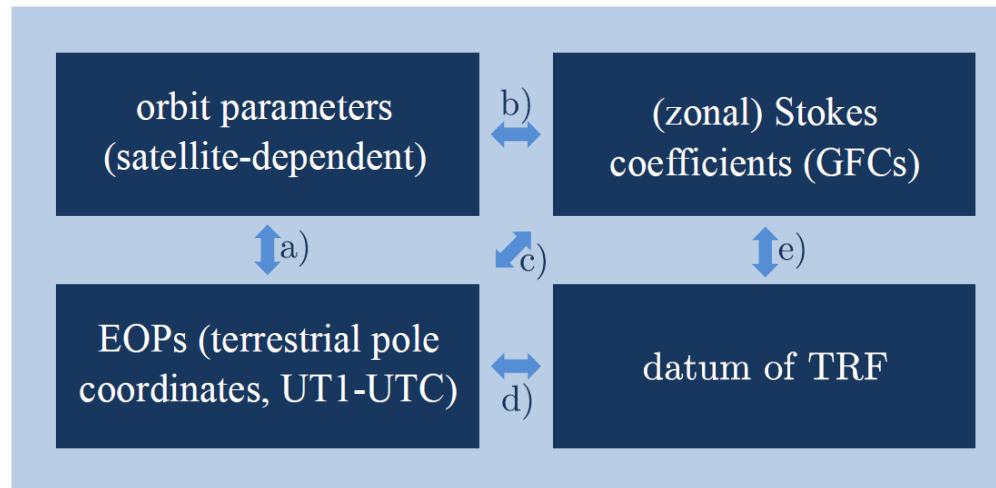


EGSIEM consortium meeting  
Bern, Switzerland, 20 January 2017



# Motivation

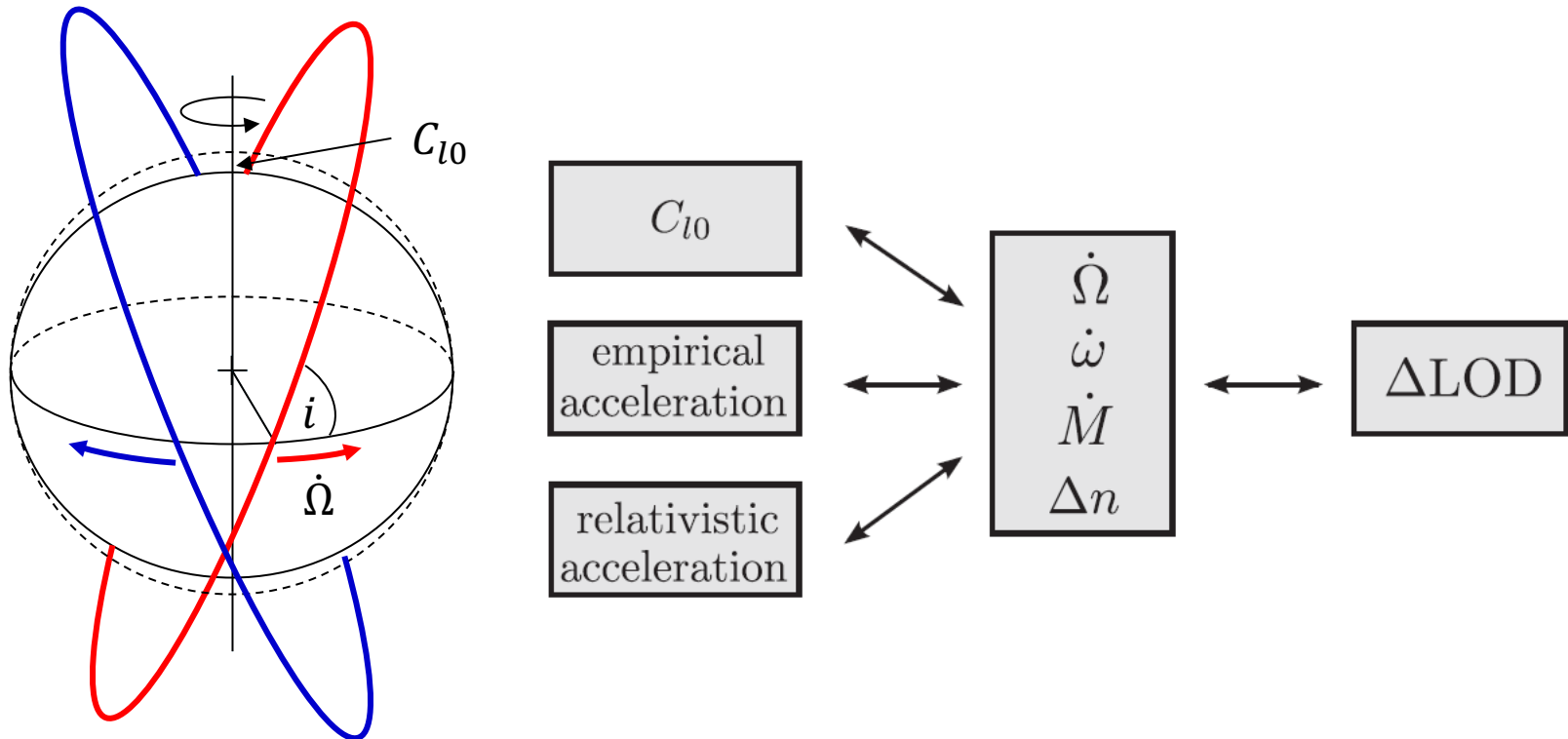
- Due to the high sensitivity of SLR observations to the fundamental geodetic parameters, correlations falsify reliable estimates



- Correlations related to Stokes coefficients
  - b) correlations of orbit parameters and Stokes coefficients
  - c) correlations of LOD and  $C_{l0}$ ;  $x_p/y_p$  with  $C_{21}/S_{21}$
  - e) correlation of TRF scale with  $C_{00}$ ; origin with  $C_{10}/C_{11}/S_{11}$ ; orientation with  $C_{21}/S_{21}/C_{22}/S_{22}$

# Motivation

- ❑ Single-satellite solution: high correlation of various parameters (especially between zonal coefficients, satellite orbit parameters and LOD)



- Multi-satellite solution (MSS): de-correlation of parameters due to combination of inclinations (e.g.  $C_{10}$  and  $\Omega$ )  $\rightarrow$  reliable estimates of zonal coefficients

# SLR decorrelation and sensitivity tests (I)

- In order to obtain reliable estimates of the Stokes coefficients, it is essential to decorrelate the orbital parameters and the coefficients of the Earth's gravitational field.
- **Test 1:** De-correlation of orbit parameters and  $C_{20}$  (taken from Bloßfeld et al., 2015)

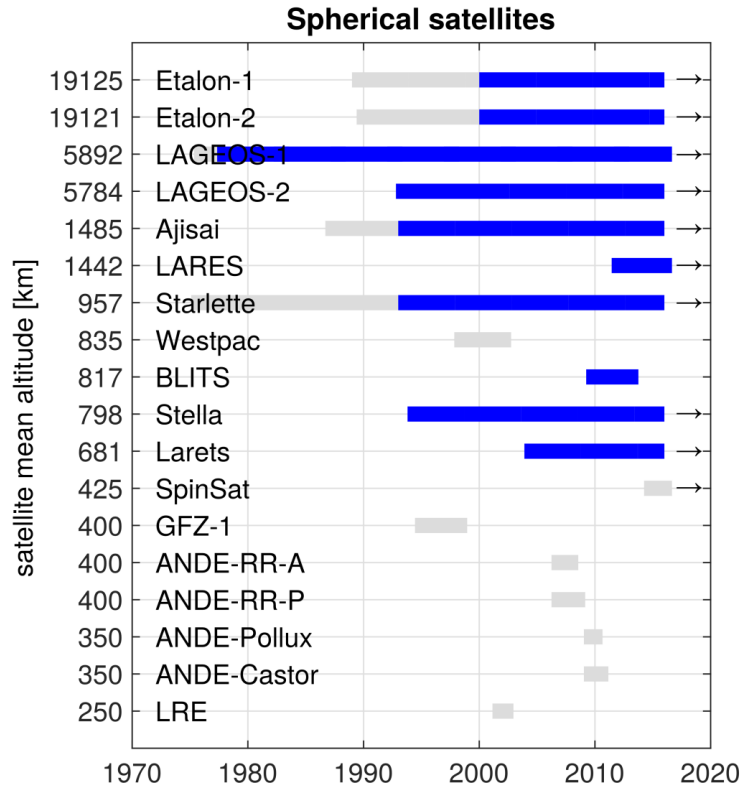
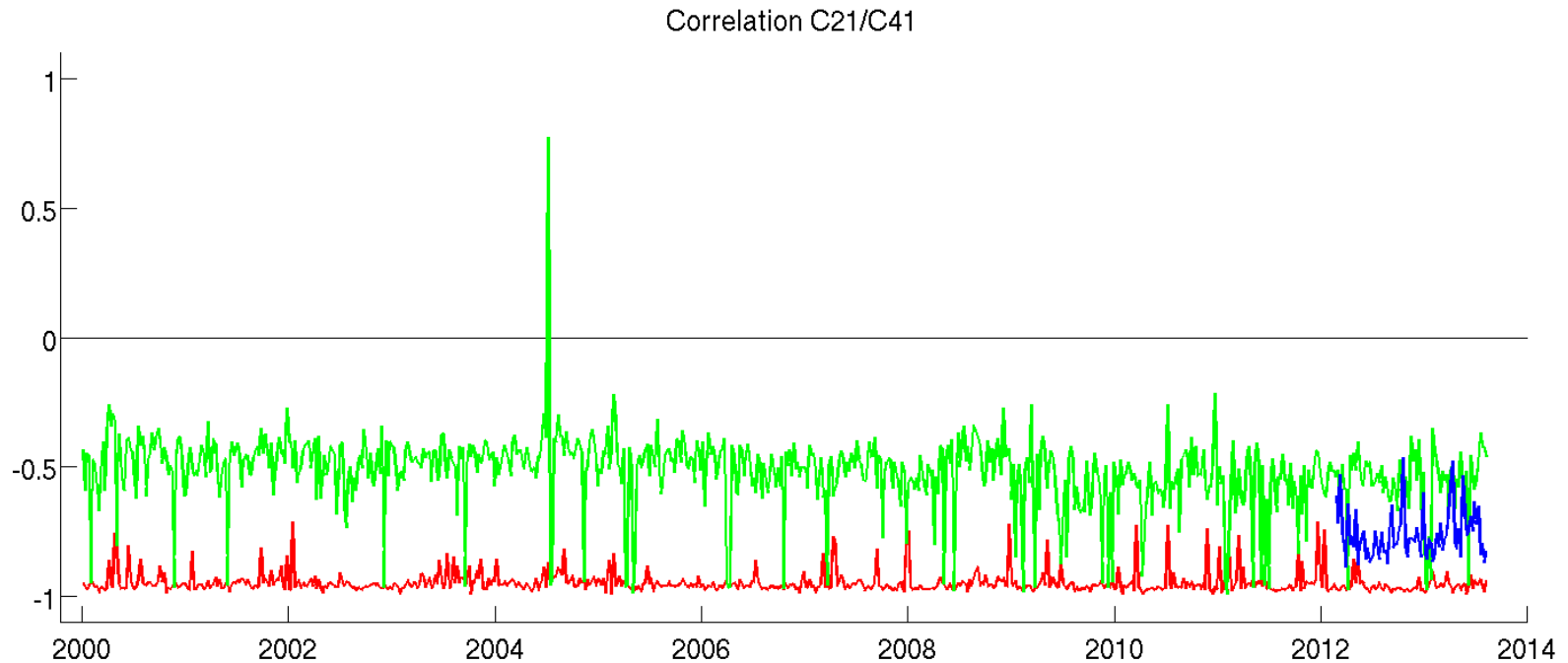


Table 8 Correlation coefficients of  $C_{20}$  and the right ascension of the ascending node of LA1 ( $\Omega_{LA1}$ ) at CW 51 of 2012.

solution	correlation coefficient
LA1	1.00
2-sat.	0.44
4-sat.	0.44 (current ILRS setup)
4-sat. + AJI	0.24
4-sat. + STA	0.28
4-sat. + STE	0.31
4-sat. + LTS	0.41
4-sat. + BTS	0.43
4-sat. + LRS	0.24 (future ILRS setup)
6-sat.	0.24
7-sat.	0.22
8-sat.	0.21
9-sat.	0.21
10-sat.	0.08

# SLR decorrelation and sensitivity tests (II)

- In order to obtain reliable estimates of the Stokes coefficients, it is essential to decorrelate the orbital parameters and the coefficients of the Earth's gravitational field.
- **Test 2:** De-correlation of different Stokes coefficients using multi-satellite SLR solution



■ LA 1/2, ET 1/2    ■ LA 1/2, ET 1/2, AJI    ■ 10 satellites

# SLR decorrelation and sensitivity tests (III)

- In order to obtain reliable estimates of the Stokes coefficients, it is essential to decorrelate the orbital parameters and the coefficients of the Earth's gravitational field.
- **Test 3:** Sensitivity analysis w.r.t. Stokes coefficients
- This test is based on the PhD thesis of R. Floberghagen (2002);

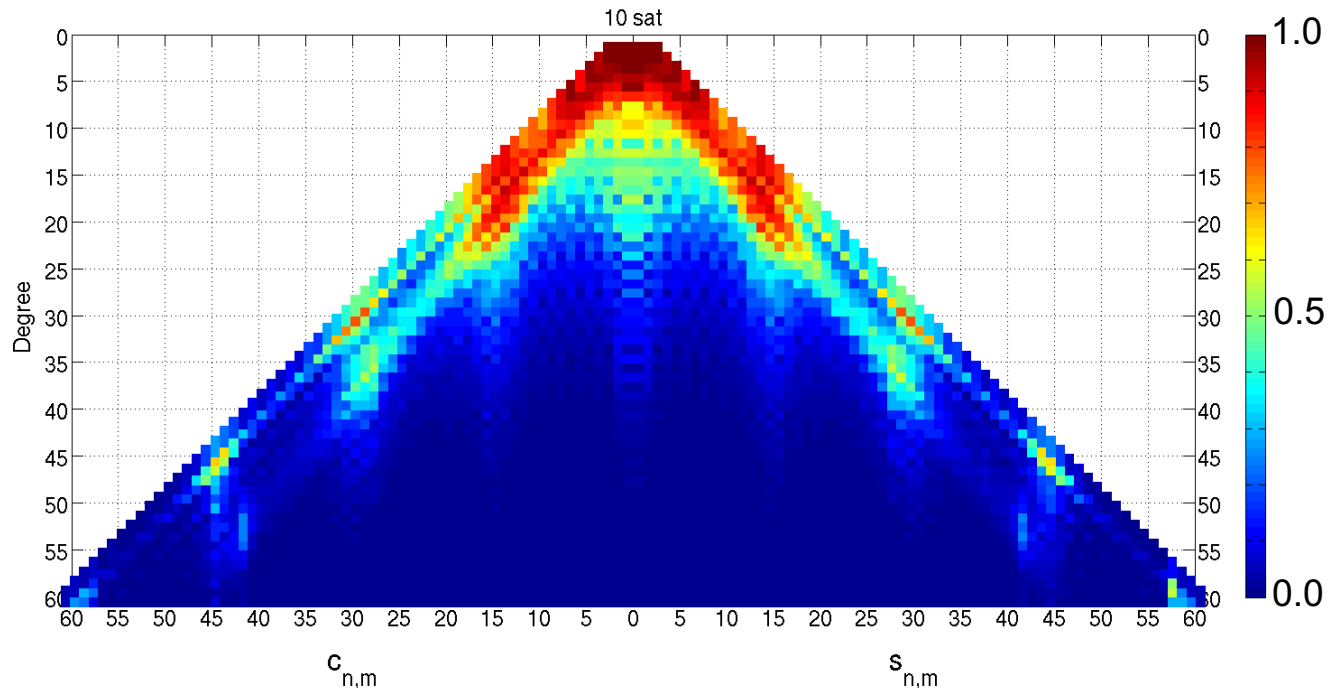
$$[0; 1] \in \text{diag}(N^{-1}N) = (A^T P A + \alpha K)^{-1} (A^T P A)$$

- **Important:** sensitivity coefficient equal to one means that the Stokes coefficient is fully determinable from the observations
- **BUT:** some coefficients are highly correlated (Haberkorn et al., 2014) and therefore only a linear combination of them (Kaula, 1966) can be estimated (e.g., even zonal low degree Stokes coefficients)

# SLR decorrelation and sensitivity tests (III)

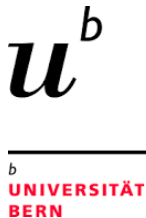
- In order to obtain reliable estimates of the Stokes coefficients, it is essential to decorrelate the orbital parameters and the coefficients of the Earth's gravitational field.
- **Test 3:** Sensitivity analysis w.r.t. Stokes coefficients

LA 1/2  
 + ET 1/2  
 + AJI  
 + STA  
 + STE  
 + LTS  
 + BTS  
 + LRS  
 + JA2



# Possible contributions to EGSIEM (by DGFI-TUM)...

- ❑ DGFI-TUM can provide SLR normal equations (NEQs) ...
  - ... which comprise SLR observations to **numerous spherical and/or non-spherical satellites**
  - ... which cover the time interval from **1978 until 2017** (laser data)
  - ... which are based on various arc lengths (**weekly, 2-weekly, monthly**)
  - ... which include station coordinates/EOP/**Stokes coefficients**/etc...
  - ... which are based on **numerous different a priori models** (solid Earth/ocean tides, non-tidal loading effects, relativistic effects, etc...)
  
- ❑ BUT: not only DGFI-TUM is able to contribute to EGSIEM with SLR data!
- ❑ A. Jäggi invited a group of (European) institutes which have SLR expertise to contribute to EGSIEM



HITOTSUBASHI UNIVERSITY







# EGSIEM SLR processing standards

- ❑ in order to be most consistent with the EGSIM processing standards for GRACE, we compiled a table summarizing all existing SLR solution setups
  
- ❑ **General information**
  - institution, software package, contact, online availability, major reference
  
- ❑ **SLR-specific corrections and solution setup**
  - time span, SLR (+DORIS) satellites, arc length, covariance information, weighting of observations, integrator details (step size), polynomial representation degree, tropospheric model, CoM correction at satellite, applied relativistic effects, applied empirical accelerations, Earth gravity field estimates
  
- ❑ **Station coordinates, gravitational perturbation, dynamic a priori models**
  - a priori station coordinates, range/time biases (SLR specific), applied constrain on station coordinates, station-dependent weighting of observations, solid Earth tides (gravity + loading), ocean tides (gravity + loading), atmospheric tides (gravity + loading), ocean pole tides (gravity + loading), a priori gravity model (static + time-variable part), C21/S21 a priori values, equatorial radius, non-tidal loading corrections (gravity + loading), lunar gravity, ephemerides

# EGSIEM SLR processing standards

- ❑ in order to be most consistent with the EGSIEM processing standards for GRACE, we compiled a table summarizing all existing SLR solution setups
  
- ❑ **Non-gravitational perturbations**
  - solar radiation, satellite drag modelling, Earth albedo, atmospheric/thermospheric model for LEOs, thermal dissipation, used satellite macromodels
  
- ❑ **EOP**
  - LOD, terrestrial mean pole, terrestrial pole
  
- ❑ rough cross-checking with GRACE processing standards (together with U. Meyer)

# EGSIEM SLR processing standards

□ potential important (critical) issues w.r.t. EGSIEM GRACE processing standards

institution	estimate d/o 1 terms	maximum d/o	apply AOD at observation level	non-unify a priori dynamic models	constrain GFCs	number of satellites	maximum time span
DGFI-TUM	no	5 + C61/S61	possible (gravity + loading)	EOT11a	unconstrained	13	1978.6 – now
AIUB/BKG	no	10	possible (gravity + loading)	EOT11a	constrained for d/o > 6	12	2002.0 – now
GFZ	yes	50	not applied	FES2004	unconstrained	6	2002.0 – now
WUELS	?	6	possible (gravity + loading)	EOT11a	?	6	?
OEAW	<b>(yes)</b>	<b>10 (in 1<sup>st</sup> iteration) and more</b>	<b>any NT-L model applied (gravity + loading)</b>	<b>any</b>	<b>unconstrained</b>	<b>4 - 13</b>	<b>2006.0 – 2008.0</b>
GRGS							
Hitotsubashi University	no	4	loading (ERA -> ATM/ CWS, ECCO -> OCN)	EOT11a	unconstrained	6	1992.8 – now
CSR	no	5 + C61/S61	not clear what was applied	?	unconstrained	4	1992.8 – 2011.4
NASA GSFC	no	5 + C61/S61	ECMWF based	GOT4.8	unconstrained	7 (SLR) + 6 (DORIS)	1992.8 – now

# Roadmap for SLR contribution to EGSIEM

- How will the SLR contribution to EGSIEM be organized?
  - Collect solution setups of SLR ACs and discuss potential/necessary unification at EGSIEM meeting in Bern (**mid of January 2017**) → send SLR processing standards to A. Jäggi
  - 1<sup>st</sup> reprocessing of singular NEQs of 2006/2007 using common standards and submission (SINEX file with NEQ and SOLUTION/ESTIMATE block) to DGFI-TUM (**end of February 2017**)
  - Generation of solutions and 1<sup>st</sup> comparisons; potential re-iteration with ACs (**end of April 2017**)
  - 2<sup>nd</sup> reprocessing (if necessary) and submission of final singular NEQs to DGFI-TUM (**mid of June 2017**)
  - Final evaluation of solutions and submission of individual AC SLR-NEQs to AIUB (including weight suggestions) for combination at NEQ level with GRACE (**end of July 2017**)
  - (Extension of time series to maximum time span)

# Combined SLR-derived gravity fields for EGSIEM

Mathis Bloßfeld, Andrea Grahl, Daniel König, Krzysztof Sosnica, Sandro Krauss,  
Rolf König, Jean-Michel Lemoine, Toshimichi Otsubo

Deutsches Geodätisches Forschungsinstitut (DGFI-TUM)  
Technische Universität München



EGSIEM consortium meeting  
Bern, Switzerland, 20 January 2017

